

Article

## Regression analysis on different mitogenic pathways

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### Abstract

In this paper different regression analysis methods were discussed on three different mitogenic pathways i.e. ERK, MK2 and JNK. Coefficient of determination, ANOVA, T-value, Durban-Watson statistics were calculated for the corresponding three proteins. The model was made using linear modeling using different regression analysis techniques in which different parameters like Mean sq error, Root mean sq error, Mean abs error, Relative sq error, Root relative sq error and Relative abs error were calculated using different analysis like PLS, linear, SVM, random forest etc were calculated. In all respect results with ERK are the best.

**Keywords** regression analysis; ERK; JNK; MK2.

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### 1 Introduction

MAP kinases are actually a family of protein kinases (Jain, 2012; Janes et al., 2005; Suzanne et al., 2005; Weiss, 2001) that are widely distributed and are found in all eukaryotic organisms. The MAPKs is divided (Jain et al., 2009; Kyriakis et al., 1996; Pearson et al., 2001) into three families as Extracellular-regulated kinase (ERK) (Jain et al., 2010), p38/high osmolarity glycerol (HOG)/Mitogen-activated protein kinase 2 (MK2) (Jain et al., 2010), stress-activated protein kinase (JNK/SAPK) (Jain, et al 2010; Jain, 2014), which leads to cell death/ cell survival. The ERK are activated by differentiation and mitogenic signals while JNK & MK2 are respond to stress and inflammaton.

ERK pathway is activated by the binding of SOS with Grb2 which results in SOS. SOS then activates RAS which leads RAF. RAF activates MEK1 and MEK2 which further activates ERK1 and ERK 2 respectively (Jain et al., 2010). The second most widely studied MAP kinase cascade is the c-Jun NH2-terminal kinase/stress activated protein kinase (JNK/ SAPK) (Brockhaus et al., 1990; Jain, 2014). The JNK are activated when cells are exposed to ultraviolet radiation, heat shock, or inflammatory cytokines. The p38/ MK2 kinase is the well-characterized member of the MAP kinase family. It is activated in response to inflammatory cytokines, endotoxins, and osmotic stress.

In this paper we will study regarding the regression analysis of different MAPK pathways. We have calculated the mean sq error, root mean sq error, mean abs error, relative sq error, root relative sq error and relative abs error using different analysis like PLS, linear, SVM, random forest etc. Coefficient of determination, ANOVA, T-value, Durban-Watson statistics were also calculated for the corresponding three proteins

## 2 Materials and Methods

In this paper we are using different regression analysis methods on different MAPK pathways i.e., ERK, MK2 and JNK. Ten different concentrations for TNF (Brockhaus et al., 1990; Jain et al., 2011), EGF (Jain, 2015; Libermann et al., 1984; Normanno et al., 2006) and Insulin (Jain, 2011, 2015; Lizcano et al., 2002) were used in ng/ml, i.e., 0-0-0, 5-0-0, 100-0-0, 0-100-0, 5-1-0, 100-100-0, 0-0-500, 0.2-0-1, 5-0-5, 100-0-500.

A) Calculation of coefficient of determination and Durban Watson statistics:

We have calculated the values of coefficient of determination and Durban Watson statistics for three proteins (ERK, MK2 and JNK) which are the main proteins for MAPK pathway. Equation 1 gives the regression coefficient ( $r^2$ ) equation.

$$r^2 = 1 - \frac{\sum (y_i - f_i)^2}{\sum (y_i - \bar{y})^2} \quad \text{or} \quad r^2 = \frac{\sum (f_i - \bar{f})^2}{\sum (y_i - \bar{y})^2} \quad (1)$$

where  $y_i$  are the observed values,  $f_i$  are the predicted values,  $\bar{y}$  are the mean values of observed data and  $\bar{f}$  are the mean values of the predicted data. If the regression model is perfect, error sum of square (SSE) is equal to zero, and its  $r^2$  is 1. If the regression model is not perfect,  $SS_E$  is equal to  $SS_T$  and its  $r^2$  is zero. Inputs are ten different concentrations of TNF- EGF - Insulin (0-0-0, 5-0-0, 100-0-0, 0-100-0, 5-1-0, 100-100-0, 0-0-500, 0.2-0-1, 5-0-5, 100-0-500) All are ng/ml. Outputs are ERK or JNK or MK2 values.

For our data sets of ten concentrations of TNF/EGF/ Insulin for ERK pathway values are as:  $S = 0.005931$ , regression coefficient ( $r^2$ ) = 92.2%,  $r^2_{(adj)}$  = 92.0%,  $r^2_{(pred)}$  = 91.6%, PRESS = 0.010980, Durbin-Watson Statistics = 2.04.

For our data sets of ten concentrations of TNF/EGF/ Insulin for MK2 pathway values are as:  $S = 0.006480$ ,  $r^2 = 90.7\%$ ,  $r^2_{(adj)}$  = 90.4%,  $r^2_{(pred)}$  = 90.01%, PRESS = 0.013055, Durbin Watson Statistics = 2.09.

For our data sets of ten concentrations of TNF/EGF/ Insulin for JNK are as:  $S = 0.01042$ , ( $r^2$ ) = 76.0%, adjusted regression coefficient ( $r^2_{(adj)}$ ) = 75.2%,  $r^2_{(pred)}$  = 74.19%, PRESS = 0.033734, Durbin Watson Statistics = 1.61.

B) Calculation of Analysis of Variance (ANOVA) (Table 1, 2 and 3):

**Table 1** Analysis of Variance (ANOVA) for all combinations of ERK.

Source	df	SS	MS	F
Regression	10	0.120516 (SSa)	0.012052 (MSa)	342.60
Residual Error	289	0.010166 (SSe)	0.000035 (MSe)	
Total	299	0.130683		

**Table 2** Analysis of Variance (ANOVA) for all combinations of MK2.

Source	df	SS	MS	F
Regression	10	0.118548 (SSa)	0.011855 (MSa)	282.33
Residual Error	289	0.012135 (SSe)	0.000042 (MSe)	
Total	299	0.130683		

**Table 3** Analysis of Variance (ANOVA) for all combinations of JNK.

Source	df	SS	MS	F
Regression	10	0.099332 (SSa)	0.009933 (MSa)	91.57
Residual Error	289	0.031350 (SSe)	0.000108 (MSe)	
Total	299	0.130682		

Table 1, Table 2 and Table 3 shows the mean squares of the regression, sum of squares and residual error for ERK, MK2 & JNK respectively. Table 4, Table 5 & Table 6 shows the standard error coefficient value,  $T$ -value,  $p$ -value,  $f$ -value which was also calculated for ERK, MK2 & JNK respectively. In these tables, SS is the sum of square, df is the degree of freedom, MS is the mean square,  $SS_a$  is the sum of square among groups,  $SS_e$  is the error sum of square,  $MS_a$  is the average variability among groups,  $MS_e$  is the average variability within groups. They are calculated as:  $MS_a = SS_a/df$ ,  $MS_e = SS_e/df$ ,  $F = MS_a/MS_e$

**Table 4** Regression analysis in terms of standard error coefficients,  $p$  value,  $T$ -value,  $F$ -value for ERK.

Effect	Coefficient	Standard Error Coefficient	t-value	p-value	VIF (variance inflation factor)
Constant	0.34684	0.02003	17.32	0.000	
0-0-0	0.00013307	0.00005417	2.46	0.015	35.0
5-0-0	0.00014586	0.00007029	2.08	0.039	8.7
100-0-0	0.00020099	0.00007236	2.78	0.006	97.1
0-100-0	0.00009306	0.00005560	1.67	0.095	21.4
5-1-0	0.00001065	0.00006060	0.18	0.861	10.6
100-100-0	0.00001734	0.00006432	0.27	0.788	77.3
0-0-500	0.00010723	0.00007165	1.50	0.136	77.4
0.2-0-1	0.00009634	0.00004255	2.26	0.024	129.5
5-0-5	0.00004758	0.00001973	2.41	0.016	247.3
100-0-500	0.00001964	0.00004623	0.42	0.671	168.9

**Table 5** Regression analysis in terms of standard error coefficients, *p* value, *T*-value, *F*- value for MK2.

Effect	Coefficient	Standard Error Coefficient	t-value	p- value	VIF (variance inflation factor)
Constant	0.59869	0.03739	16.01	0.000	
0-0-0	0.00002453	0.00005234	0.47	0.640	1.7
5-0-0	-0.00004073	0.00005098	-0.80	0.425	2.1
100-0-0	-0.00033461	0.00003862	-8.67	0.000	13.7
0-100-0	0.00000636	0.00004956	0.13	0.898	2.0
5-1-0	0.00010052	0.00005540	1.81	0.071	4.1
100-100-0	-0.00001375	0.00004750	-0.29	0.772	23.2
0-0-500	0.00003543	0.00005259	0.67	0.501	15.5
0.2-0-1	0.00009931	0.00004462	2.23	0.027	9.9
5-0-5	-0.00027582	0.00004681	-5.89	0.000	18.9
100-0-500	-0.00007383	0.00004397	-1.68	0.094	33.0

**Table 6** Regression analysis in terms of standard error coefficients, *p* value, *T*-value, *F*- value for JNK.

Effect	Coefficient	Standard Error Coeff	T-Value	p- Value	F- Value
0-0-0	0.92309	0.04895	18.86	0.000	
5-0-0	0.00012979	0.00008235	1.58	0.116	1.6
100-0-0	-0.00023739	0.00008791	-2.70	0.007	1.5
0-100-0	-0.00075872	0.00006467	-11.73	0.000	1.6
5-1-0	-0.00000557	0.00008274	-0.07	0.946	1.0
100-100-0	-0.00038617	0.00007818	-4.94	0.000	1.8
0-0-500	0.00009802	0.00008049	1.22	0.224	1.2
0.2-0-1	0.00004452	0.00008060	0.55	0.581	1.0
5-0-5	-0.00042354	0.00008249	-5.13	0.000	4.2
100-0-500	-0.00004693	0.00008336	-0.56	0.574	1.6

We clubbed all the concentrations of TNF, EGF and Insulin and only normalized output (ERK, MK2, JNK) were taken and we get the regression equation as:

$$\text{Final Output for ERK} = 0.347 + 0.000133 a + 0.000146 b + 0.000201 c + 0.000093 d + 0.000011 e + 0.000017 f + 0.000107 g + 0.000096 h + 0.000048 i + 0.000020 j \quad (2)$$

$$\text{Final Output for MK2} = 0.599 + 0.000025 a - 0.000041 b - 0.000335 c + 0.000006 d + 0.000101 e - 0.000014 f + 0.000035 g + 0.000099 h - 0.000276 i - 0.000074 j \quad (3)$$

$$\text{Final Output for JNK} = 0.923 + 0.000130a - 0.000237b - 0.000759c - 0.000006d - 0.000386e + 0.000098f + 0.000045g - 0.000424h - 0.000047i - 0.000154j. \quad (4)$$

where a, b, c are the different concentrations of TNF, EGF and Insulin.

We have calculated mean sq error (MSE), root mean sq error (RMSE), mean abs error (MAE), relative sq error (RSE), root relative sq error (RRSE) and relative abs error (RAE) for ERK, MK2 and JNK using different regression analysis like PLS, linear, SVM, KNN, random forest, regression etc was given in Table 7, Table 8 and Table 9 respectively.

- Mean square error: where  $f_i$  is the predicted value and  $y_i$  is the actual/ observed value

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_i - f_i)^2 \quad (5)$$

- Root mean sq error: RMSE is used to measure the error rate of a regression model. However, it can only be compared between models whose errors are measured in the same units.

$$RMSE = \sqrt{\frac{1}{n} \sum_{i=1}^n (y_i - f_i)^2} \quad (6)$$

- Mean abs error: MAE has the same unit as the original data, and it can only be compared between models whose errors are measured in the same units. It is usually similar in magnitude to RMSE, but slightly smaller.

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_i - f_i| \quad (7)$$

- Relative sq error: RSE can be compared between models whose errors are measured in the different units.

$$RSE = \frac{\sum_{i=1}^n (y_i - f_i)^2}{\sum_{i=1}^n (\bar{y} - f_i)^2} \quad (8)$$

- Root relative sq error:

$$RRSE = \sqrt{\frac{\sum_{i=1}^n (y_i - f_i)^2}{\sum_{i=1}^n (\bar{y} - f_i)^2}} \quad (9)$$

- Relative abs error: RAE can be compared between models whose errors are measured in the different units.

$$RAE = \frac{\sum_{i=1}^n |y_i - f_i|}{\sum_{i=1}^n |\bar{y} - f_i|} \quad (10)$$

**Table 7** Various parameters using different regression methods for ERK.

	<b>MSE</b>	<b>RMSE</b>	<b>MAE</b>	<b>RSE</b>	<b>RRSE</b>	<b>RAE</b>
<b>PLS Regression</b>	0.0000	0.0060	0.0048	0.0836	0.2891	0.2551
<b>Linear Regression</b>	0.0000	0.0060	0.0048	0.0836	0.2891	0.2551
<b>SVM Regression</b>	0.0005	0.0216	0.0207	1.0755	1.0371	1.0969
<b>K nearest neighbours regression</b>	0.0001	0.0072	0.0058	0.1189	0.3448	0.3089
<b>Mean</b>	0.0004	0.0210	0.0190	1.0125	1.0062	1.0042
<b>Random Forest regression</b>	0.0000	0.0065	0.0052	0.0964	0.3105	0.2727
<b>Regression tree</b>	0.0000	0.0060	0.0048	0.0840	0.2898	0.2557

**Table 8** Various analysis parameters using diff regression methods for MK2.

	<b>MSE</b>	<b>RMSE</b>	<b>MAE</b>	<b>RSE</b>	<b>RRSE</b>	<b>RAE</b>
<b>PLS Regression</b>	0.0000	0.0067	0.0054	0.1017	0.3190	0.2847
<b>Linear Regression</b>	0.0000	0.0067	0.0054	0.1017	0.3190	0.2847
<b>SVM Regression</b>	0.0005	0.0216	0.0207	1.0755	1.0371	1.0969
<b>K nearest neighbours regression</b>	0.0001	0.0072	0.0058	0.1187	0.3445	0.3058
<b>Mean</b>	0.0004	0.0210	0.0190	1.0125	1.0062	1.0042
<b>Random Forest regression</b>	0.0000	0.0070	0.0055	0.1113	0.3336	0.2888
<b>Regression tree</b>	0.0000	0.0060	0.0048	0.0840	0.2898	0.2557

**Table 9** Various analysis parameters using diff regression methods for JNK.

	<b>MSE</b>	<b>RMSE</b>	<b>MAE</b>	<b>RSE</b>	<b>RRSE</b>	<b>RAE</b>
<b>PLS Regression</b>	0.0001	0.0106	0.0085	0.2599	0.5098	0.4521
<b>Linear Regression</b>	0.0001	0.0106	0.0085	0.2599	0.5098	0.4521
<b>SVM Regression</b>	0.0005	0.0216	0.0207	1.0755	1.0371	1.0969
<b>K nearest neighbors regression</b>	0.0001	0.0093	0.0066	0.2004	0.4477	0.3517
<b>Mean</b>	0.0004	0.0210	0.0190	1.0125	1.0062	1.0042
<b>Random Forest regression</b>	0.0001	0.0088	0.0067	0.1763	0.4199	0.3552
<b>Regression tree</b>	0.0000	0.0069	0.0051	0.1104	0.3323	0.2692

### 3 Conclusion

In this paper we have discussed the coefficient of determination, ANOVA, T-value, Durban Watson statistics, P-value, F-value, standard error coefficients for different mitogenic pathways, i.e., JNK, ERK, and MK2. We have also calculated MSE, RMSE, MAE, RSE, etc., using different analysis methods like PLS, linear, SVM, random forest etc. In all respect results with ERK are the best. In future we will find the pdf all proteins using different distribution functions.

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