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# Regression modeling of different proteins using linear and multiple analysis 

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#### Abstract

There are different types of regression analysis. Out of which simple regression and multiple regressions was considered in this paper. For calculation purpose we have used PLS analysis which calculates squared $r$ values. This paper considers eleven different proteins and one output. We have validated our results by calculating adjusted regression coefficient, predicted regression coefficient regression coefficient cross validation, $\mathrm{rm}^{2}$ and $F$-test values. Later multiple regressions were used as we have different independent variable (proteins). For that analysis we have calculated the coefficient, standard error, standard coefficient, tolerance, $t$ value and $p$ value, variation explanation of predictors and estimators which gives percentage and cumulative percentage. Correlation matrixes were also shown at the end for eleven proteins and one output.


Keywords linear regression analysis; multiple regression analysis; marker proteins; PLS.

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## 1 Introduction

Regression analysis (RA) is a statistical method for investigating relationship between one variable and other variables (Farahani, 2010; Ringle, 2010). A statistical model is a simple description of state. There are three types of RA: linear regression (LR), multiple linear regression (MLR) and non linear regression (NLR). If we have to model the linear relationship between dependent and independent variables than LR was used but if there are more than one independent variable and one dependent variable than MLR is used. The MLR considers co linearity, variance inflation, graphical display of regression diagnosis, and detection of regression outlier and influential observation. In NLR the variables (dependent and independent) are not linear. NLR can be written as

$$
\begin{equation*}
y=\frac{\alpha}{1+e^{\beta t}}+\varepsilon \tag{1}
\end{equation*}
$$

where $y$ is the growth of a particular organism as a function of time $t, \alpha$ and $\beta$ are model parameters, and $\varepsilon$ is
the random error. NLR model is more complicated than LR model in terms of estimation of model parameters, model selection, model diagnosis, variable selection, outlier detection, or influential observation identification. In this paper we have calculated regression coefficient or regression coefficient cross validation ( $r^{2}$ or $q^{2}$ cv), adjusted regression coefficient ( $r_{\text {adj }}^{2}$ ), predicted regression coefficient ( $r_{\text {pre }}^{2}$ ), regression coefficient without intercept ( $r^{2}{ }_{0}$ ) for ten different concentration (Jain, 2012a; Suzzane, 2005; Weiss, 2001) of three input proteins TNF (Thoma, 1990; Jain, 2009a, 2009b, 2010a, 2011a), EGF (Janes, 2005; Normano, 2006; Jain, 2014, 2015a, 2016a, 2017) and Insulin (Jain, 2010b, 2010c, 2011b, 2012b, 2012c; Morris, 2003). For validation of our results we have calculated $r m^{2}$ and $F$-test values. Different plots were plotted which are showing $r^{2}$ values. Later in paper we have shown the results of multiple regression. We have different marker proteins: AkT (Coffer, 1998; Hemmings, 1997; Bruent, 1999; Jain, 2010d, 2012d, 2015b, 2017b), MK2 (Jain, 2011c, 2016b, 2016c), JNK (Jain, 2010e, 2015b, 2015c), FKHR (Jain, 2015c, 2011d), MEK, ERK, IRS, IKK, pAkT, ptAkT and EGFR for the HT carcinoma cells which helps in cell survival/ apoptosis. If these proteins are present in the pathway than it leads to cell survival otherwise cell death (Jain, 2009c).

## 2 Material and Methods

There are different types of regression analysis. In this paper we are working on Linear Regression/ Simple regression (LR) and Multiple regression analysis (MR). For calculation of LR there are two techniques: Ordinary least square method (OLS) and Partial least square method (PLS). PLS is a technique which is helpful in predictive models when the factors are many and highly collinear. PLS approach is beneficial for relating dependent variables to many independent variables.

LR as the name suggests the shape of regression line is linear whose intercept is $a$ and slope of line is $b$. For LR the dependent variable $(Y)$ is continuous while independent variable ( $X$ ) can be continuous or discrete. We can consider the error term ' $e$ or $\varepsilon$ '. LR is expressed as:

$$
\begin{equation*}
\underbrace{Y}_{\text {actual(observed) }}=\underbrace{a X+b}_{\text {explained (predicted) }}+\underbrace{\varepsilon_{1}}_{\text {error }} \tag{2}
\end{equation*}
$$

Equation 1 is also known as linear population regression model, or linear population regression. For LR error $\varepsilon$ is normally distributed with $E(\varepsilon)=0$ and a constant variance $\operatorname{Var}(\varepsilon)=\sigma^{2}$. LR can be also be represented as :

$$
\begin{equation*}
\underbrace{\underline{Y}}_{\text {observed }}=\underbrace{\hat{Y}}_{\text {predicted/estimator }}+\underbrace{\hat{\varepsilon}}_{\text {error/residual }} \tag{3}
\end{equation*}
$$

Predicted value is also known as conditional mean. For predicted values equation 2 can be written as:

$$
\begin{equation*}
\hat{Y}=\hat{a} X+\hat{b} \tag{4}
\end{equation*}
$$

Equation 4 is known as sample regression function (SRF) where intercept is represented by equation 5.

$$
\begin{equation*}
\hat{b}=\bar{Y}-\hat{a} \bar{X} \tag{5}
\end{equation*}
$$

$\bar{X}$ and $\bar{Y}$ are the sample means of $X$ and $Y$. Slope is represented as:

$$
\begin{gather*}
\hat{a}=\frac{S S_{X Y}}{S S_{X X}}=\frac{\sum(X-\bar{X})(Y-\bar{Y})}{\sum(X-\bar{X})^{2}}=\frac{\sum x y}{\sum x^{2}}=\frac{\operatorname{Cov}(X, Y)}{\operatorname{Var}(X)}  \tag{6}\\
\operatorname{Cov}(X, Y)=\operatorname{Var}(X, Y)=\frac{\sum(X-\bar{X})(Y-\bar{Y})}{n-1}
\end{gather*}
$$

where

$$
\operatorname{Var}(X)=\frac{\sum(X-\bar{X})^{2}}{n-1} \quad \operatorname{Var}(Y)=\frac{\sum(Y-\bar{Y})^{2}}{n-1}
$$

and
equation 6 can be written as

$$
\begin{equation*}
\hat{a}=\frac{\sum x Y}{\sum X^{2}-n \bar{X}^{2}}=\frac{\sum X y}{\sum X^{2}-n \bar{X}^{2}} \tag{7}
\end{equation*}
$$

We can define $x=(X-\bar{X})$ and $y=(Y-\bar{Y})$ where lower case letters denote deviations from mean values.

OLS method and PLS is used for calculation of LR. OLS minimizes the SS of the vertical deviations from each data point to the line while in PLS, initially the values are squared, then added up so as there is no cancellation of positive and negative terms. Finally, the minimum (least) square value is considered. We have three different types of sum of squares (SS):
a. regression sum of squares (SSreg) / explained SS which is a measure of explained variation,

$$
\begin{equation*}
S S_{\text {reg }}=\sum(\hat{y}-\bar{y})^{2} \tag{8}
\end{equation*}
$$

b. residual sum of squares or error sum of squares $\left(\mathrm{SS}_{\text {err }}\right)$ / unexplained SS which is a measure of unexplained variation and

$$
\begin{equation*}
S S_{\text {err }}=S S_{\text {residual }}=\sum(y-\hat{y})^{2}=\sum \hat{\varepsilon}^{2} \tag{9}
\end{equation*}
$$



$$
\begin{align*}
& S S_{\text {total }}=S S_{\text {reg }}+S S_{\text {err }}  \tag{10}\\
& S S_{\text {total }}=\sum(y-\bar{y})^{2} \tag{11}
\end{align*}
$$

The ratio of $S S_{\text {reg }}$ to $S S_{\text {total }}$ is known as coefficient of determination $\left(r^{2}\right)$ is expressed as:

$$
\begin{equation*}
r^{2}=\frac{S S_{r e g}}{S S_{\text {total }}}=\frac{S S_{\text {reg }}}{S S_{\text {reg }}+S S_{e r r}}=1-\frac{S S_{e r r}}{S S_{\text {total }}} \tag{12}
\end{equation*}
$$

For deviation form, the SRF can be written as:

$$
\begin{align*}
& =\frac{\sum \hat{y}^{2}}{\sum y^{2}}  \tag{13}\\
& =\frac{\hat{a}^{2} \sum x^{2}}{\sum y^{2}}  \tag{14}\\
& =\hat{a}^{2}\left(\frac{\sum x^{2}}{\sum y^{2}}\right) \tag{15}
\end{align*}
$$

If numerator and denominator are divided by sample size ' $n$ ' than $r^{2}$ is expressed as:

$$
\begin{equation*}
r^{2}=\hat{a}^{2}\left(\frac{S_{x}^{2}}{S_{y}^{2}}\right)=a^{2}\left(\frac{\operatorname{Var} X}{\operatorname{Var} Y}\right) \tag{16}
\end{equation*}
$$

where $S_{\mathrm{x}}{ }^{2}$ and $S_{\mathrm{y}}{ }^{2}$ is a sample variance of $X$ and $Y$ respectively.
Replace the value of $\hat{a}$ in equation 15 by equation 6 ; we get

$$
\begin{align*}
& r^{2}=\frac{\left(\sum x y\right)^{2}}{\sum x^{2} \sum y^{2}}  \tag{17}\\
& r=\frac{\left(\sum x y\right)}{\sqrt{\sum x^{2} \sum y^{2}}}=\frac{\operatorname{Cov}(X, Y)}{\sqrt{\operatorname{Var}(X) \cdot \operatorname{Var}(Y)}} \tag{18}
\end{align*}
$$

In above equation; $r$ is known as sample/linear correlation coefficient. Equation 12 can be written as $S S_{\text {reg }}=r^{2} S S_{\text {total }}$ where

$$
\begin{equation*}
S S_{\text {total }}=\sum y^{2} \tag{19}
\end{equation*}
$$

Equation 10 can be written as

$$
\begin{equation*}
S S_{\text {reg }}=r^{2} \sum y^{2} \tag{20}
\end{equation*}
$$

$$
S S_{\mathrm{err}}=S S_{\text {total }}-S S_{\text {reg }}
$$

Placing values from eq 19 and eq 20 to equation 10 we get:

$$
\begin{equation*}
S S_{e r r}=\sum y^{2}\left(1-r^{2}\right) \tag{21}
\end{equation*}
$$

Finally, placing all the values i.e. from eq 19 , eq 20 and eq 21 in equation 120 we get

$$
\begin{equation*}
\sum y^{2}=r^{2} \sum y^{2}+\sum y^{2}\left(1-r^{2}\right) \tag{22}
\end{equation*}
$$

The $r^{2}$ lies in the range of 0 and 1 , greater the value of $r^{2}$ more accurate the model. If the value of $r^{2}$ is 1 means
a perfect fit on the other hand if $r^{2}$ value is zero it means that there is no relationship between regress and regressor. $r^{2}$ is a measure of goodness of fit which tells how close the estimate values are to their actual values. $r^{2}$ can also be calculated as the squared coefficient of correlation between actual $Y$, estimated $Y$ i.e. $\hat{Y}$ and is expressed as

$$
\begin{gather*}
r^{2}=\frac{\sum(Y-\bar{Y})^{2}(\hat{Y}-\bar{Y})^{2}}{\sum(Y-\bar{Y})^{2} \sum(\hat{Y}-\bar{Y})^{2}}  \tag{23}\\
=\frac{\left(\sum y \hat{y}\right)^{2}}{\sum y^{2} \sum \hat{y}^{2}} \tag{24}
\end{gather*}
$$

Multiple Regression (MR): If the $x$ parameters are more than one i.e. $x_{1}, x_{2} \ldots$ than the regression analysis is known as multiple regression (MR) but if the $x$ parameter is one than it is LR. MR equation can be represented as:

$$
\begin{equation*}
y=a+b_{1} x_{1}+b_{2} x_{2}+b_{3} x_{3}+\ldots b_{\mathrm{n}} x_{\mathrm{n}}+e \tag{25}
\end{equation*}
$$

For MR it is usually assumed that the error term $\varepsilon$ follows the normal distribution with $\mathrm{E}(\varepsilon)=0$ and a constant variance $\operatorname{Var}(\varepsilon)=\sigma^{2}$. Forward selection (FS), backward elimination (BE) and step wise approximation (SWA) is used for analysis of MR.

## 3 Validation Tests

In this paper we are considering LR and MR methods for which we have discussed how to calculate $r^{2}$ values. To validate the results we have different approaches. In this paper we are using $r_{\text {adj, }}^{2}, r_{\text {pre, }}^{2} q^{2}{ }_{\text {cv }}, r m^{2}$ and $F$-test values. The predictive capability of the equation is determined using the leave-one-out cross validation method. $q^{2}{ }_{\mathrm{cv}}$ was calculated by the following equation:

$$
\begin{equation*}
q_{c v}^{2}=1-\frac{P R E S S}{T O T A L} \approx r^{2} \tag{26}
\end{equation*}
$$

For a perfect model value of $q^{2}{ }_{c v}$ should be close to one and its value is approximately equal to $r^{2}$.

The evaluation of the predictive ability of the model for the external test set compounds was done by determining the value of $r m^{2}$ which was determine by :

$$
\begin{equation*}
r m^{2}=r^{2}\left(1-\left|\sqrt{r^{2}-r_{0}^{2}}\right|\right) \tag{27}
\end{equation*}
$$

$r_{0}^{2}$ is the squared correlation coefficient for regression without using intercept and the regression equation becomes $y=a x$. For a perfect model value of $r m^{2}$ should be close to one.

## 4 Discussion

In this paper we have considered eleven different proteins MK2, JNK, FKHR, MEK, ERK, IRS, AkT, IKK,
pAkT, ptAkT and EGFR for the HT carcinoma cells which occurs due to the combination of TNF, EGF and Insulin. These proteins yield four different output: phosphatidylserine exposure (PE), membrane permeability (MP), nuclear fragmentation (NF) and caspase substrate cleavage (CCK). We have first taken average of all outputs and then normalized the output to maximum that's why in results we are showing only one output. Table 1 shows the minimum, maximum, median, mean, standard deviation, variance, and coefficient of variance for eleven different proteins and output.

Table 1 Different values for eleven different proteins and output.

|  | MK2 | JNK | FKHR | MEK | ERK | IRS | AKT | IKK | pAKT | pTAKT | EGFR | OUTPUT |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| N of Cases | 300 | 300 | 300 | 300 | 300 | 300 | 300 | 300 | 300 | 300 | 300 | 300 |
| Minimum | 221.466 | 221.526 | 191.019 | 110.233 | 140.711 | 191.123 | 164.909 | 59.976 | 110.359 | 90.321 | 49.437 | 0.407 |
| Maximum | 262.76 | 255.651 | 245.391 | 189.092 | 189.29 | 244.545 | 188.985 | 90.748 | 201.321 | 133.322 | 78.153 | 0.593 |
| Median | 242.156 | 235.749 | 210.593 | 136.447 | 172.221 | 216.314 | 177.376 | 76.804 | 157.058 | 108.792 | 68.604 | 0.48 |
| Arithmetic <br> Mean | 242.798 | 236.224 | 214.208 | 144.297 | 167.113 | 216.768 | 177.868 | 75.085 | 154.684 | 110.499 | 64.849 | 0.483 |
| Standard | 10.541 | 8.302 | 14.94 | 26.971 | 14.425 | 14.304 | 6.149 | 9.22 | 30.922 | 13.876 | 9.505 | 0.051 |
| Deviation |  |  |  |  |  |  |  |  |  |  |  |  |
| Variance | 111.115 | 68.923 | 223.217 | 727.422 | 208.083 | 204.606 | 37.808 | 85.006 | 956.141 | 192.552 | 90.348 | 0.003 |
| Coefficient <br> of Variation | 0.043 | 0.035 | 0.07 | 0.187 | 0.086 | 0.066 | 0.035 | 0.123 | 0.2 | 0.126 | 0.147 | 0.106 |

In this section we have shown all the results $r^{2}, r_{\text {adj }}^{2}, q^{2}{ }_{\mathrm{cv}}, r m^{2}$ and $F$-test values for our 10 data sets of TNF/ EGF and Insulin in ng/ml.

1. For $r^{2}$ : We have observed values of our 10 data set. First we have predicted the values using STAT SOFT software. We have put all results in excel and get the $r^{2}$ value from their and then calculate the same $r^{2}$ value using formula as shown in Eq 1 . We have also calculated the $r^{2}$ value using MINITAB software. All the results of $r^{2}$ are shown in Table 2 which proves that all the values are same.

Table 2 All possible values of $r^{2}$ using excel, formula and software.

| S. No | Possible Values | $\boldsymbol{r}^{2}$ from excel | $\boldsymbol{r}^{2}$ from formula <br> using equation 1 | $\boldsymbol{r}^{2}$ from <br> software |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $0-0-0$ | 0.984 | 0.984 | 0.985 |
| $\mathbf{2}$ | $5-0-0$ | 0.991 | 0.991 | 0.991 |
| $\mathbf{3}$ | $100-0-0$ | 0.966 | 0.966 | 0.966 |
| $\mathbf{4}$ | $0-100-0$ | 0.765 | 0.8265 | 0.765 |
| $\mathbf{5}$ | $5-1-0$ | 0.953 | 0.9589 | 0.953 |
| $\mathbf{6}$ | $100-100-0$ | 0.981 | 0.9817 | 0.981 |
| $\mathbf{7}$ | $0-0-500$ | 0.991 | 0.992 | 0.991 |
| $\mathbf{8}$ | $0.2-0-1$ | 0.985 | 0.985 | 0.985 |
| $\mathbf{9}$ | $5-0-5$ | 0.9916 | 0.992 | 0.992 |
| $\mathbf{1 0}$ | $100-0-500$ | 0.9105 | 0.9116 | 0.911 |

2. For $\boldsymbol{r}_{\text {pred, }}^{2} \boldsymbol{r}_{\text {adj }}^{2}$ : We have calculated the $r_{\text {pred, }}^{2} r^{2}$ adj using MINITAB software shown in Table 3 which is coming out to be OK. Table 4 shows the cumulative $r^{2}$ values for $X$ and $Y$. this table also represents the Eigen values and $Q^{2}$ cumulative values.

Table 3 Values of $r^{2}, r_{\text {pred }}^{2}, r_{\text {adj }}^{2}$.

| S. No | Possible Values | $\boldsymbol{r}^{\mathbf{2}}$ <br> $\mathbf{( \% )}$ | $\boldsymbol{r}_{\text {pred }}$ <br> $\mathbf{( \% )}$ | $\boldsymbol{r}_{\text {adj }}$ <br> $\mathbf{( \% )}$ |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $0-0-0$ | 98.5 | 98.5 | 98.49 |
| $\mathbf{2}$ | $5-0-0$ | 99.1 | 99.13 | 99.1 |
| $\mathbf{3}$ | $100-0-0$ | 96.6 | 96.59 | 96.6 |
| $\mathbf{4}$ | $0-100-0$ | 76.5 | 76.44 | 76.5 |
| $\mathbf{5}$ | $5-1-0$ | 95.3 | 95.32 | 95.3 |
| $\mathbf{6}$ | $100-100-0$ | 98.1 | 98.10 | 98.1 |
| $\mathbf{7}$ | $0-0-500$ | 99.1 | 99.10 | 99.1 |
| $\mathbf{8}$ | $0.2-0-1$ | 98.5 | 98.49 | 98.5 |
| $\mathbf{9}$ | $5-0-5$ | 99.2 | 99.16 | 99.2 |
| $\mathbf{1 0}$ | $100-0-500$ | 91.1 | 91.05 | 91.1 |

Table 4 Eigen values and cumulative Q2 values of ten different concentrations.

| S. No | Possible <br> Values | $\boldsymbol{r}^{\mathbf{2}} \mathbf{~}$ <br> (Cumul.) | Eigen <br> values | $\boldsymbol{r}^{\mathbf{Y}}$ <br> (Cumul.) | $\boldsymbol{Q}^{\mathbf{2}}$ <br> (Cumul.) | Iterations |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{1}$ | $0-0-0$ | 0.661527 | 6.778547 | 0.642263 | 0.530556 | 3 |
| $\mathbf{2}$ | $5-0-0$ | 0.706644 | 7.770976 | 0.664049 | 0.662104 | 4 |
| $\mathbf{3}$ | $100-0-0$ | 0.716885 | 7.654734 | 0.70051 | 0.648019 | 6 |
| $\mathbf{4}$ | $0-100-0$ | 0.643378 | 6.55393 | 0.589539 | 0.48238 | 5 |
| $\mathbf{5}$ | $05-01-2000$ | 0.449319 | 4.906164 | 0.515036 | 0.460442 | 49 |
| $\mathbf{6}$ | $100-100-0$ | 0.704479 | 7.743815 | 0.663912 | 0.661397 | 4 |
| $\mathbf{7}$ | $0-0-500$ | 0.794276 | 8.711558 | 0.517066 | 0.512291 | 4 |
| $\mathbf{8}$ | $0.2-0-1$ | 0.76338 | 8.297655 | 0.704509 | 0.685306 | 3 |
| $\mathbf{9}$ | $5-0-5$ | 0.806147 | 8.854371 | 0.482898 | 0.480075 | 4 |
| $\mathbf{1 0}$ | $100-0-500$ | 0.658964 | 7.232619 | 0.6151 | 0.609608 | 9 |

3. For $\boldsymbol{q}^{2}$ cv: As we know for a perfect model value of $q^{2}$ cv should be close to one and its value should be equal to $r^{2}$. We have already calculated the value of $r^{2}$. $q^{2}{ }_{\mathrm{cv}}$ is calculated from MINITAB software both the values are equal. So it proves that the value of $q^{2}{ }_{c v}$ is close to $r^{2}$.
4. For rm${ }^{2}$ : Fig. 1 shows the $r^{2}$ and $r^{2}{ }_{0}$ value for ten different concentrations. For $r^{2}$ and $r^{2}{ }_{0}$ value we have plotted the observed value and predicted value in Excel and get the equations from the same. Similarly we have plotted the data in MINITAB software and get the same equation which verifies the result as shown in Table 5. Putting the values of $r^{2}$ and $r^{2}{ }_{0}$ in Eq. 27 we get the $r m^{2}$ value which is coming close to one as shown in Table 6 which verifies our result.



Fig. 1 Values for $r^{2}$ and $r^{2}{ }_{0}$ for 10 data sets.

Table 5 Equations of $r^{2}$ and $r^{2}{ }_{0}$.

| S. No | Possible Values | $\boldsymbol{r}^{2}$ with intercept <br> From excel | $\boldsymbol{r}^{2}$ with intercept <br> From MINITAB | $\boldsymbol{r}^{2}{ }_{0}$ without intercept |
| :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $0-0-0$ | $0.9849 x+2.3484$ | $0.985 x+2.35$ | $0.9972 x$ |
| $\mathbf{2}$ | $5-0-0$ | $0.9913 x+1.429$ | $0.991 x+1.43$ | $0.9989 x$ |
| $\mathbf{3}$ | $100-0-0$ | $0.9659 x+5.7226$ | $0.966 x+5.72$ | $0.9937 x$ |
| $\mathbf{4}$ | $0-100-0$ | $0.765 x+45.605$ | $0.765 x+45.6$ | $0.9765 x$ |
| $\mathbf{5}$ | $5-1-0$ | $0.9533 x+8.2958$ | $0.953 x+8.30$ | $0.9954 x$ |
| $\mathbf{6}$ | $100-100-0$ | $0.981 x+3.2371$ | $0.981 x+3.24$ | $0.9967 x$ |
| $\mathbf{7}$ | $0-0-500$ | $0.9911 x+1.6992$ | $0.991 x+1.7$ | $0.9984 x$ |
| $\mathbf{8}$ | $0.2-0-1$ | $0.9849 x+2.6647$ | $0.985 x+2.66$ | $0.9975 x$ |
| $\mathbf{9}$ | $5-0-5$ | $0.9916 x+1.7447$ | $0.992 x+1.74$ | $0.9964 x$ |
| $\mathbf{1 0}$ | $100-0-500$ | $0.9105 x+14.806$ | $0.911 x+14.8$ | $0.9792 x$ |

Table 6 Values of $\mathrm{rm}^{2}$.

| S. No | Possible Values | $\boldsymbol{r}^{\mathbf{2}}$ | $\boldsymbol{r}_{\mathbf{2}}$ | $\mathbf{r m}^{2}$ <br> $($ close to 1) | $\left(\boldsymbol{r}^{2}-\boldsymbol{r}_{\mathbf{0}}^{\mathbf{0}}\right) / \boldsymbol{r}^{2}$ <br> $($ less than 0.1) |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $0-0-0$ | 0.984 | 0.9847 | 0.970971 | 0.0002 |
| $\mathbf{2}$ | $5-0-0$ | 0.991 | 0.9912 | 0.981387 | 0.0001 |
| $\mathbf{3}$ | $100-0-0$ | 0.966 | 0.9649 | 0.935356 | 0.00104 |
| $\mathbf{4}$ | $0-100-0$ | 0.765 | 0.7 | 0.569963 | 0.08497 |
| $\mathbf{5}$ | $5-1-0$ | 0.953 | 0.9512 | 0.909614 | 0.0022 |
| $\mathbf{6}$ | $100-100-0$ | 0.981 | 0.9807 | 0.964009 | 0.00031 |
| $\mathbf{7}$ | $0-0-500$ | 0.991 | 0.991 | 0.981189 | 0.0001 |
| $\mathbf{8}$ | $0.2-0-1$ | 0.985 | 0.9847 | 0.970971 | 0.0002 |
| $\mathbf{9}$ | $5-0-5$ | 0.9916 | 0.9915 | 0.981684 | 0.0001 |
| $\mathbf{1 0}$ | $100-0-500$ | 0.9105 | 0.9038 | 0.835972 | 0.00736 |

5. For $\boldsymbol{F}$-value: With the help of observed and predicted values we have calculated $F$-value shown in Table 7 which is coming out to be very large.

Table 7 Values of $F$-value.

| S. <br> No | Possible <br> Values | PRESS | F-value |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $0-0-0$ | 273446 | 215195.4 |
| $\mathbf{2}$ | $5-0-0$ | 106089 | 375401.5 |
| $\mathbf{3}$ | $100-0-0$ | 698648 | 93465.53 |
| $\mathbf{4}$ | $0-100-0$ | 2484216 | 10735.86 |
| $\mathbf{5}$ | $5-1-0$ | 505386 | 97249.82 |
| $\mathbf{6}$ | $100-100-0$ | 382434 | 170650 |
| $\mathbf{7}$ | $0-0-500$ | 235785 | 365494 |
| $\mathbf{8}$ | $0.2-0-1$ | 296709 | 215009.8 |
| $\mathbf{9}$ | $5-0-5$ | 896652 | 388299.1 |
| $\mathbf{1 0}$ | $100-0-500$ | 2231417 | 33567.88 |

As the independent variables are many so MR can be applied. Table 8 shows the coefficient, standard coefficient, $t$ value and $p$ values of the independent variables. Table 9 shows the variation explanation for predictors and responses of eleven proteins and output. Table 10 shows the correlation matrixes for eleven different proteins and one output.

Table 8 Different parameters for MR.

| Predictor | Coeff | SE coeff | $\boldsymbol{t}$ | $\boldsymbol{p}$ |
| :---: | :---: | :---: | :---: | :---: |
| Constant | 0.2225 | 0.187 | 1.19 | 0.235 |
| MK2 | 0.001157 | 0.000186 | 6.21 | 0 |
| JNK | -0.00046 | 0.000222 | -2.07 | 0.039 |


| FKHR | -0.0007 | 0.000232 | -3.03 | 0.003 |
| :---: | :---: | :---: | :---: | :---: |
| MEK | -0.00045 | 0.000296 | -1.5 | 0.133 |
| ERK | 0.001518 | 0.000306 | 4.97 | 0 |
| IRS | 0.000117 | 0.000249 | 0.47 | 0.639 |
| AkT | -0.00124 | 0.00027 | -4.6 | 0 |
| IKK | -0.00033 | 0.000624 | -0.53 | 0.597 |
| pAkT | -0.00122 | 0.000266 | -4.58 | 0 |
| ptAkT | 0.001206 | 0.000423 | 2.85 | 0.005 |
| EGFR | 0.005013 | 0.000674 | 7.44 | 0 |

Table 9 Variation explained for predictors and responses of eleven proteins.

| Factors | Variation Explained for |  | Variation Explained for |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Predictor(s) |  | Response(s) |  |
|  | Percentage | Cum. Percentage | Percentage | Cum. Percentage |
| MK2 | 68.938 | 68.938 | 45.166 | 45.166 |
| JNK | 14.369 | 83.307 | 22.41 | 67.576 |
| FKHR | 4.333 | 87.64 | 3.151 | 70.727 |
| MEK | 2.077 | 89.717 | 3.485 | 74.212 |
| ERK | 4.783 | 94.5 | 0.648 | 74.86 |
| IRS | 2.176 | 96.675 | 0.639 | 75.499 |
| AkT | 0.797 | 97.473 | 0.221 | 75.72 |
| IKK | 0.971 | 98.443 | 0.042 | 75.763 |
| pAkT | 0.738 | 99.181 | 0.017 | 75.779 |
| ptAkT | 0.287 | 99.468 | 0.002 | 75.781 |
| Output | 0.532 | 100 | 0 | 75.781 |

Table 10 Correlation matrixes.

|  | MK2 | JNK | FKHR | MEK | ERK | IRS | AKT | IKK | PAKT | PTAKT | EGFR | OUTPUT |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| MK2 | 1 |  |  |  |  |  |  |  |  |  |  |  |
| JNK | -0.026 | 1 |  |  |  |  |  |  |  |  |  |  |
| FKHR | 0.226 | 0.511 | 1 |  |  |  |  |  |  |  |  |  |
| MEK | 0.263 | 0.538 | 0.895 | 1 |  |  |  |  |  |  |  |  |
| ERK | -0.223 | -0.533 | -0.85 | -0.934 | 1 |  |  |  |  |  |  |  |
| IRS | 0.366 | 0.442 | 0.8 | 0.876 | -0.831 | 1 |  |  |  |  |  |  |
| AKT | -0.313 | 0.163 | 0.108 | 0.105 | -0.135 | 0.029 | 1 |  |  |  |  |  |
| IKK | -0.295 | -0.515 | -0.875 | -0.955 | 0.909 | -0.888 | -0.08 | 1 |  |  |  |  |
| PAKT | -0.377 | -0.517 | -0.882 | -0.966 | 0.917 | -0.899 | -0.043 | 0.954 | 1 |  |  |  |
| PTAKT | 0.364 | 0.507 | 0.865 | 0.947 | -0.903 | 0.884 | 0.035 | -0.938 | -0.962 | 1 |  |  |
| EGFR | -0.218 | -0.564 | -0.889 | -0.963 | 0.925 | -0.865 | -0.162 | 0.937 | 0.945 | -0.929 | 1 |  |
| OUTPUT | 0.306 | -0.497 | -0.596 | -0.6 | 0.637 | -0.444 | -0.442 | 0.546 | 0.497 | -0.487 | 0.666 | 1 |

## 5 Conclusion

We have made a best fit linear model using partial least square for ten cytokine combinations of TNF, EGF and Insulin. In this we have find all the results like regression coefficient, adjusted regression coefficient, regression coefficient cross validation, $\mathrm{rm}^{2}$ and $F$-test values for our 10 data sets which comes out to be correct. Later multiple regressions were applied as we have eleven different input independent variables (proteins). We have calculated coefficient, standard error, standard coefficient, tolerance, $t$ value and $p$ value, variation explanation of predictors and estimators which gives percentage and cumulative percentage of all eleven proteins and one output. Later, Correlation matrixes were also for eleven proteins and one output.

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