

Article

Delayed control of ecological and biological networks

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Abstract

Evolutionary Network Control (ENC) was introduced in 2011 to permit the control of any kind of ecological and biological networks, with an arbitrary number of nodes and links. To date, ENC has been applied with the idea to control biological and ecological networks since the beginning of their system dynamics. This approach has shown to be effective in the control of both continuous-time and discrete-time networks. However a delayed control, where network dynamics are controlled only from a certain point on, could be more economic from a computational viewpoint, and also more feasible from an applicative perspective. For this reason, ENC is further upgraded here to realize the delayed control of ecological and biological nets.

Keywords delayed network control; dynamical networks; genetic algorithms; Euclidean distance; network optimization; system dynamics.

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1 Introduction

Evolutionary Network Control (ENC; Ferrarini, 2011) has been conceived to enable the control of any kind of ecological and biological networks, with an arbitrary number of nodes and links, from inside (Ferrarini, 2013) and from outside (Ferrarini, 2013b). The endogenous control requires that the network is optimized at the beginning of its dynamics so that it will inertially go to the desired state. Instead, the exogenous control requires that one or more exogenous controllers act upon the network at each time step.

ENC makes use of an integrated solution (system dynamics - genetic optimization - stochastic simulations) to compute uncertainty about network control (Ferrarini, 2013c) and to compute control success and feasibility (Ferrarini, 2013d). ENC opposes the common idea in the scientific literature that controllability of networks should be based on the identification of the set of driver nodes that can guide the system's dynamics (Ferrarini, 2011), in other words on the choice of a subset of nodes that should be selected to be permanently controlled. ENC has been applied to both discrete-time (systems of difference equations) and continuous-time (systems of differential equations) networks.

ENC employs intermediate control functions to locally (step-by-step) drive ecological and biological networks, so that also intermediate steps (not only the final state) are under its strict control (Ferrarini, 2014).

ENC can also globally subdue nonlinear networks (Ferrarini, 2015), impose early or late stability to any kind of ecological and biological network (Ferrarini 2015b) and locally control nonlinear networks (Ferrarini 2016).

ENC has been also expanded to incorporate the multipurpose control of any kind of ecological and biological network (Ferrarini, 2016b). The rationale is that, not one, but at least two, or even more than two, variables can be contemporaneously driven towards the desired equilibrium values. It is useful whenever ecological and biological networks present several taxonomic resolutions that are worthy to be controlled simultaneously.

A decentralized variant of ENC (Ferrarini, 2016c), where only one node and the correspondent input/output links are controlled, has been also introduced as it could be more economic from a computational viewpoint, in particular when the network is very large (i.e. big data).

A further ENC variant, based on the inhibition of one or several nodes and/or edges, permits to more easily and parsimoniously subdue biological and ecological networks (Ferrarini, 2016d). Another task of ENC is the control of network flows at equilibrium (Ferrarini, 2017).

To date, ENC has been applied with the idea in mind to control biological and ecological networks since the beginning of their system dynamics. However a delayed control, where network dynamics are controlled only from a certain point on, could be more economic from a computational viewpoint, and also more feasible from an applicative perspective. For this reason, ENC has been further upgraded here to realize the delayed control of ecological and biological nets.

Table 1 Evolutionary Network Control (ENC) and its applications.

Reference	Goal
Ferrarini 2011	Theoretical bases of Evolutionary Network Control
Ferrarini 2013	Endogenous control of linear ecological and biological networks
Ferrarini 2013b	Exogenous control of linear ecological and biological networks
Ferrarini 2013c	Computing the uncertainty associated with network control
Ferrarini 2013d	Computing the degree of success and feasibility of network control
Ferrarini 2014	Local control of linear ecological and biological networks
Ferrarini 2015	Global control of nonlinear ecological and biological networks
Ferrarini 2015b	Imposing early/late stability to linear and nonlinear networks
Ferrarini 2016	Local control of nonlinear ecological and biological networks
Ferrarini 2016b	Multipurpose control of ecological and biological networks
Ferrarini 2016c	Decentralized control of ecological and biological networks
Ferrarini 2016d	Structural control of ecological and biological networks
Ferrarini 2017	Control of network flows at equilibrium
This work	Delayed control of ecological and biological networks

2 Delayed Evolutionary Network Control: Mathematical Formulation

An ecological (or biological) dynamical system of n interacting taxonomic resolutions (species, genera, family, etc.) or aggregated assemblages of taxa (e.g., phytoplankton) is as follows

$$\frac{d\mathbf{S}}{dt} = \gamma(\mathbf{S}(t)) \quad (1)$$

where $S_i \in \mathbf{S}$ is the number of individuals (or the total biomass) of the generic i -th taxonomic resolution (species, genera, family, or aggregated assemblages of taxa). If we also consider inputs (e.g. immigration) and outputs (e.g. emigration) from-to outside, we must write:

$$\frac{d\mathbf{S}}{dt} = \gamma(\mathbf{S}(t)) + \mathbf{I}(t) + \mathbf{O}(t) \quad (2)$$

At the beginning of its dynamics, the network values are

$$\mathbf{S}_0 = \langle S_1(0), S_2(0) \dots S_n(0) \rangle \quad (3)$$

while at the generic time t

$$\mathbf{S}_t = \langle S_1(t), S_2(t) \dots S_n(t) \rangle \quad (4)$$

Now let's introduce a desired solution at equilibrium for the dynamics of the studied network

$$\mathbf{S}_d = \langle S_1(d), S_2(d) \dots S_n(d) \rangle \quad (5)$$

At each time step, the distance between \mathbf{S}_t and \mathbf{S}_d can be computed as Euclidean distance in the n -dimension space of the n -variable network dynamics:

$$Dist(\mathbf{S}_t, \mathbf{S}_d) = \sqrt{(S_{1t} - S_{1d})^2 + (S_{2t} - S_{2d})^2 + \dots + (S_{nt} - S_{nd})^2} \quad (6)$$

Now, let's introduce a desired threshold distance T_d which triggers the activation of the evolutionary network control (ENC) as follows:

$$\left\{ \begin{array}{l} \text{IF } Dist(\mathbf{S}_t, \mathbf{S}_d) > T_d \\ \text{THEN ENC is off} \\ \text{ELSE ENC is on} \end{array} \right. \quad (7)$$

In other words, ENC is activated if, and only if, the ecological and biological net under study is sufficiently near to the desired solution at equilibrium.

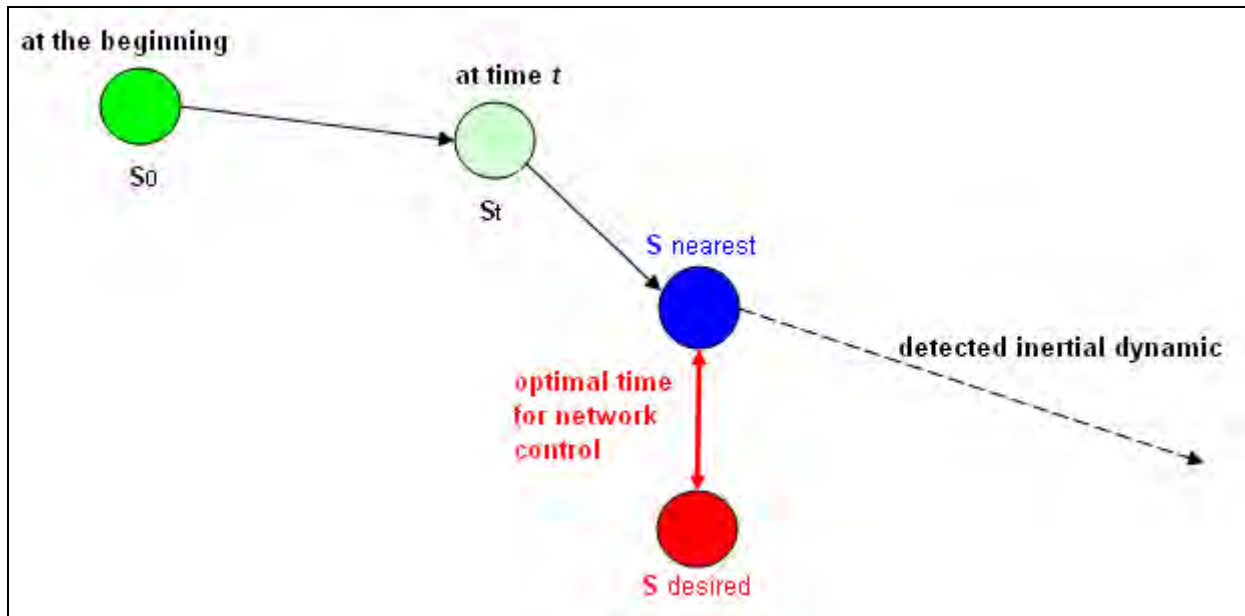


Fig. 1 The idea behind Delayed Evolutionary Network Control (D-ENC). Rather than controlling network dynamics since their beginning, D-ENC seeks the optimal time (T_{opt}) to activate network control. The optimal time happens when network dynamics are closer to the desired solution than a pre-defined threshold value. At that point in time, ENC activates to drive the ecological/biological network towards the desired solution.

Once that ENC is on, it solves the control of Eq. 2 using the following approach (Ferrarini, 2013)

$$\left\{ \begin{array}{l} \frac{dS_1}{dt} = a_{11^*}S_1^* + \dots + a_{1n^*}S_n^* + I_{1^*} + O_{1^*} \\ \dots \\ \frac{dS_n}{dt} = a_{n1^*}S_1^* + \dots + a_{nn^*}S_n^* + I_{n^*} + O_{n^*} \end{array} \right. \quad (8)$$

where any component (variable, parameter or coefficient) of Eq. 8 can be tamed, as denoted by the asterisk, using genetic optimization (Holland, 1975; Goldberg, 1989) to drive the network towards the desired state. ENC can also use an exogenous network control using an external controller C_1 (Ferrarini, 2013b)

$$\begin{cases} \frac{dS_1}{dt} = a_{11}S_1 + \dots + a_{1n}S_n + I_1 + O_1 + c_{11^*}C_{1^*} \\ \dots \\ \frac{dS_n}{dt} = a_{n1}S_1 + \dots + a_{nn}S_n + I_n + O_n + c_{n1^*}C_{1^*} \\ \frac{dC_1}{dt} = f_1S_1 + \dots + f_nS_n \end{cases} \quad (9)$$

where asterisks stand for the genetic optimization of exogenous node's edges (i.e., coefficients of interaction with the inner system) and exogenous node's stock. The controller C_l that can also receive feedbacks from the network, which could be subject to control by subduing $\langle f_l \dots f_n \rangle$. In case 1 controller is not enough, the model in (9) must be expanded to the following k -external-controllers model (Ferrarini, 2013b):

$$\begin{cases} \frac{dS_1}{dt} = a_{11}S_1 + \dots + a_{1n}S_n + I_1 + O_1 + c_{11^*}C_{1^*} + \dots + c_{1k^*}C_{k^*} \\ \dots \\ \frac{dS_n}{dt} = a_{n1}S_1 + \dots + a_{nn}S_n + I_n + O_n + c_{n1^*}C_{1^*} + \dots + c_{nk^*}C_{k^*} \\ \frac{dC_1}{dt} = f_{11}S_1 + \dots + f_{1n}S_n \\ \dots \\ \frac{dC_k}{dt} = f_{k1}S_1 + \dots + f_{kn}S_n \end{cases} \quad (10)$$

Many ecological (or biological) dynamical systems can be more properly described using difference (recurrent) equations rather than differential ones. This is true for many systems where dynamics happen on discrete, rather than continuous, time. In this case, the ruling equation becomes

$$\begin{cases} (S_1)_{t+1} = a_{11}(S_1)_t + \dots + a_{1n}(S_n)_t + (I_1)_t + (O_1)_t \\ \dots \\ (S_n)_{t+1} = a_{n1}(S_1)_t + \dots + a_{nn}(S_n)_t + (I_n)_t + (O_n)_t \end{cases} \quad (11)$$

ENC solves the control of Eq. 11 using the following approach

$$\left\{ \begin{array}{l} (S_1)_{t+1} = a_{11*}(S_1)_t + \dots + a_{1n*}(S_n)_t + (I_1)_{t*} + (O_1)_{t*} \\ \dots \\ (S_n)_{t+1} = a_{n1*}(S_1)_t + \dots + a_{nn*}(S_n)_t + (I_n)_{t*} + (O_n)_{t*} \end{array} \right. \quad (12)$$

Delayed ENC can be applied using the software Control-Lab 8 (Ferrarini, 2017b).

3 Conclusions

Evolutionary network control (ENC) has been introduced as a methodology where an arbitrary number of network nodes and links can be subdued to drive the network dynamics towards the desired outputs. In previous studies, ENC has shown to be very effective in the control of ecological and biological networks. A delayed control could be more economic from a computational viewpoint, in particular when the network is very large. In this sense, delayed ENC results very promising when applied to big data, the new frontier of network dynamics and control.

References

- Ferrarini A. 2011. Some thoughts on the controllability of network systems. *Network Biology*, 1(3-4): 186-188
- Ferrarini A. 2013. Controlling ecological and biological networks via evolutionary modelling. *Network Biology*, 3(3): 97-105
- Ferrarini A. 2013b. Exogenous control of biological and ecological systems through evolutionary modelling. *Proceedings of the International Academy of Ecology and Environmental Sciences*, 3(3): 257-265
- Ferrarini A. 2013c. Computing the uncertainty associated with the control of ecological and biological systems. *Computational Ecology and Software*, 3(3): 74-80
- Ferrarini A. 2013d. Networks control: introducing the degree of success and feasibility. *Network Biology*, 3(4): 115-120
- Ferrarini A. 2014. Local and global control of ecological and biological networks. *Network Biology*, 4(1): 21-30
- Ferrarini A. 2015. Evolutionary network control also holds for nonlinear networks: Ruling the Lotka-Volterra model. *Network Biology*, 5(1): 34-42
- Ferrarini A. 2015b. Imposing early stability to ecological and biological networks through Evolutionary Network Control. *Proceedings of the International Academy of Ecology and Environmental Sciences*, 5(1): 49-56
- Ferrarini A. 2016. Bit by bit control of nonlinear ecological and biological networks using Evolutionary Network Control. *Network Biology*, 6(2): 47-54
- Ferrarini A. 2016b. Multipurpose control of ecological and biological networks. *Proceedings of the International Academy of Ecology and Environmental Sciences*, 6(3): 75-83
- Ferrarini A., 2016c. Decentralized control of ecological and biological networks through Evolutionary Network Control. *Network Biology*, 6(3): 65-74
- Ferrarini A., 2016d. Structural control of ecological and biological networks. *Computational Ecology and Software*, 6(4): 130-138
- Ferrarini A, 2017. A deeper insight into the equilibrium of ecological and biological networks. *Network Biology*, 7(4): 98-104

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- Ferrarini A. 2017b. Control-Lab 8: a software for the application of Ecological Network Control. Manual, 108 pages (in Italian)
- Goldberg DE. 1989. Genetic Algorithms in Search Optimization and Machine Learning. Addison-Wesley, Reading, USA
- Holland JH. 1975. Adaptation in Natural And Artificial Systems: An Introductory Analysis With Applications To Biology, Control and Artificial Intelligence. University of Michigan Press, Ann Arbor, USA